Rényi Entanglement Entropy of Interacting Fermions A Continuous-time Quantum Monte Carlo Approach

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Implemented for interacting fermions [1], works better than free fermion decomposition approach [2].



References

Area law scaling of entanglement entropy implies *exponentially* vanishing Monte Carlo signal.

entanglement entropy $\Delta S_2 = -\ln \left[\eta \frac{\mathcal{Z}^A / \mathcal{Z}_0^A}{(\mathcal{Z} / \mathcal{Z}_0)^2} \right] + \ln(\eta)$ $S_2^0 = -\ln\left(\frac{\mathcal{Z}_0^A}{\mathcal{Z}_0^2}\right)$ Easily calculated by Sampled use CTQMC correlation matrix method [3] Extended ensemble simulation

[1] P. Broecker and S. Trebst, arXiv: 1404.3027

[2] T. Grover, Phys. Rev. Lett. 111, 130402 (2013)

[3] I. Peschel, J. Phys. A: Math. Gen. 36, L205 (2003)

[4] J. E. Gubernatis, D. J. Scalapino, R. L. Sugar, and W. D. Toussaint, Phys. Rev. B 32, 103 (1985)



 $(\mathcal{Z}/\mathcal{Z}_0)^2 + \eta(\mathcal{Z}^A/\mathcal{Z}_0^A)$ $= \sum \left[w_{\mathcal{Z}^2}(\mathcal{C}) + \eta w_{\mathcal{Z}^A}(\mathcal{C}) \right]$



 $\Delta S_2 = -\ln \left| \frac{\langle \delta_{\mathcal{Z}^A} \rangle_{\mathrm{MC}}}{\langle \delta_{\mathcal{Z}^2} \rangle_{\mathrm{MC}}} \right| + \ln(\eta)$

Critical Point



8-site open chain

1.6

1.4

3.0

0.4

 S_2





Square lattice t-V model undergoes an Ising phase transition to a CDW phase at large interaction or low temperature.

Mutual information crossing locates the critical point









a CDW transition [4]

V/tAgree perfectly with exact diagonalization (solid lines)



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