

$$\hat{H} = \hat{H}_{\uparrow}^0(+\phi) + \hat{H}_{\downarrow}^0(-\phi) - U \sum_i \hat{n}_{i\uparrow} \hat{n}_{i\downarrow}$$