

$$= \frac{e^{\Delta\tau U/4}}{2} \sum_{s=\pm 1} e^{i\gamma s(\hat{n}_{\mathbf{r}\uparrow} - \hat{n}_{\mathbf{r}\downarrow})}$$