

$$\hat{H} = \sum_{x,y} e^{i2\pi y\phi} \hat{c}_{x+1,y}^\dagger \hat{c}_{x,y} + \hat{c}_{x,y+1}^\dagger \hat{c}_{x,y} + h.c.$$